

2-Pole 2-Zero Transfer function For LP. (eq 45 in paper)

$$H(z) = \frac{1 + 2 \cdot z^{-1} + z^{-2}}{1 - 2 \cdot R \cdot x \cdot z^{-1} + R^2 \cdot z^{-2}}$$

$$\text{Inverse BLT } z^{-1} = \left( \frac{2-s}{2+s} \right)$$

Substituting in H(z)

$$H(z) = \frac{1 + 2 \cdot \left( \frac{2-s}{2+s} \right) + \left( \frac{2-s}{2+s} \right)^2}{1 - 2 \cdot R \cdot x \cdot \left( \frac{2-s}{2+s} \right) + R^2 \cdot \left( \frac{2-s}{2+s} \right)^2}$$

Simplifying it

$$H(s) = \frac{16}{4 - 8 \cdot R \cdot x + 4 \cdot R^2 + (4 - 4 \cdot R^2) \cdot s + (1 + 2 \cdot R \cdot x + R^2) \cdot s^2}$$

Forcing s^2 coefficient to 1 for easy solving later.

$$H(s) = \frac{\frac{16}{(1 + 2 \cdot R \cdot x + R^2)}}{\frac{4 - 8 \cdot R \cdot x + 4 \cdot R^2}{(1 + 2 \cdot R \cdot x + R^2)} + \frac{(4 - 4 \cdot R^2)}{(1 + 2 \cdot R \cdot x + R^2)} \cdot s + s^2}$$

The SVF topology has the following transfer function (eq 12 in paper):

$$G(s) = \frac{(w_c)^2}{s^2 + 2 \cdot k \cdot w_c \cdot s + w_c}$$

k here is R in the topology but I named it differently to distinguish it from the radius R in H(z)

So to equalize H(s) and G(s). Coefficients has to be equal

$$w_c = \frac{4 - 8 \cdot R \cdot x + 4 \cdot R^2}{(1 + 2 \cdot R \cdot x + R^2)} \quad 2 \cdot k \cdot w_c = \frac{(4 - 4 \cdot R^2)}{(1 + 2 \cdot R \cdot x + R^2)} \quad (w_c)^2 = \frac{16}{(1 + 2 \cdot R \cdot x + R^2)}$$

Feeding the above into a CAS results in no solution. Basically there are more equations than unknowns.

We can surely get  $Wc$  and  $k$ , but then the 3rd equation won't be satisfied.

I know we should account for the pre-warp. But that still won't solve the above as far as I can see.